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# Exchange interactions in R-Co-B (R=Y, Sm and Gd) compounds

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## Abstract

We calculated the molecular field coefficients,  $n_{RCo}$  (R=Sm and Gd) and  $n_{CoCo}$  (R=Y) for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$  using the experimental values of the Curie temperature. The  $R_{n+1}Co_{3n+5}B_{2n}$  compounds with n=1 (RCo<sub>4</sub>B), n=2 ( $R_3Co_{11}B_4$ ) and n=3 ( $R_2Co_7B_3$ ) are derived from the RCo<sub>5</sub> structure by substituting B for Co at the 2*c* site. We examined the relationships between the values of  $n_{RCo}$  and  $n_{CoCo}$  and the B, Co and R concentrations, the Co moments and the two types of volume per formula unit RCo<sub>m</sub>B<sub>n</sub> and  $R_mCo_nB$ . © 2001 Elsevier Science B.V. All rights reserved.

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# 1. Introduction

In rare-earth-transition metal (R-M) compounds, three types of exchange interactions occur: M-M, R-M and R-R. In general, in compounds where the transition metal atoms carry a well established magnetic moment, the M-M interaction dominates. It turns out to be strong enough to produce an almost exact parallel alignment of the 3d magnetic moments at low temperatures. This interaction primarily governs the temperature dependence of the 3d moment and the Curie temperature,  $T_{\rm C}$ , of a 3d-4f compound. The R-M interaction essentially determines the magnetic behavior of the rare-earth sublattice. Due to the localized character of the 4f shell, these R-M interactions are indirect, mediated by the 5d, 6s conduction electrons. The 3d-4f interaction produces a dominant contribution to the molecular field experienced by the rare-earth moments. The R-R interaction between the 4f spins is generally the weakest one in the 3d-4f compounds [1,2].

The  $R_{n+1}Co_{3n+5}B_{2n}$  compounds, where R is a rare earth or yttrium, crystallize in a hexagonal structure having the *P6/mmm* space group and are known to exhibit a very interesting series of crystal structures with special atomic orderings depending on *n* [3–5]. The  $R_{n+1}Co_{3n+5}B_{2n}$ 

compounds with n=1 (RCo<sub>4</sub>B), n=2 (R<sub>3</sub>Co<sub>11</sub>B<sub>4</sub>), n=3 (R<sub>2</sub>Co<sub>7</sub>B<sub>3</sub>) and  $n=\infty$  (RCo<sub>3</sub>B<sub>2</sub>) are derived from the RCo<sub>5</sub> structure by substituting B for Co at the 2*c* site [6]. Generally, three kinds of Co atoms are assumed for R<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub>. Co(0), Co(1) and Co(2) have zero, one and two neighboring B-layers, respectively. The RCo<sub>4</sub>B compound has Co(0) and Co(1). The R<sub>3</sub>Co<sub>11</sub>B<sub>4</sub> and R<sub>2</sub>Co<sub>7</sub>B<sub>3</sub> compounds have Co(0), Co(1) and Co(2). The RCo<sub>3</sub>B<sub>2</sub> compound has only Co(2) and the average Co moment of RCo<sub>3</sub>B<sub>2</sub> is very small [7].

The R<sub>2</sub>Co<sub>14</sub>B compound crystallizes with a tetragonal structure having the  $P4_2/mnm$  space group. The R<sub>2</sub>Fe<sub>14</sub>B compound is most attractive due to the industrial application for permanent magnets. There are four R<sub>2</sub>Co<sub>14</sub>B units (68 atoms) per unit cell. All the R and B atoms, but only four of the 56 Co atoms, reside in the z = 0 and 0.5 planes. Between these the other Co atoms form puckered, yet fully connected, hexagonal nets. The tetragonal structure of R<sub>2</sub>Co<sub>14</sub>B is closely related to the RCo<sub>5</sub>-type structure [8].

To compare the strength of the exchange interactions between R and Co spins and between Co spins for R–Co– B and related compounds, we calculated the molecular field coefficients,  $n_{\rm RCo}$  (R=Sm and Gd) and  $n_{\rm CoCo}$  (R=Y) for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$ using the experimental values of the Curie temperature. Moreover, we examined the relationships between the values of  $n_{\rm RCo}$  and  $n_{\rm CoCo}$  and those of the B, Co and R

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concentrations, the Co moment and the two types of volume per formula unit  $RCo_mB_n$  and  $R_mCo_nB$ .

#### 2. Results and discussion

The exchange interactions can be analyzed by the molecular field model, which is commonly used to describe the variation of the Curie temperature in the R–Fe intermetallic series, under the assumption that the localized 3d-electron model is applicable.

Applying the two-sublattice molecular field model to the paramagnetic state [1], the following expression can be obtained,

 $T_{\rm C} = [T_{\rm Co} + T_{\rm R} + \{(T_{\rm Co} - T_{\rm R})^2 + 4T_{\rm RCo}^2\}^{1/2}]/2,$ (1)

where

$$T_{\rm Co} = n_{\rm CoCo} C_{\rm Co}, \tag{2}$$

$$T_{\rm R} = \alpha^2 n_{\rm RR} C_{\rm R},\tag{3}$$

and

$$T_{\rm RCo} = |\alpha| n_{\rm RCo} (C_{\rm R} C_{\rm Co})^{1/2}$$
  
= {(T\_{\rm C} - T\_{\rm Co})(T\_{\rm C} - T\_{\rm R})}<sup>1/2</sup>. (4)

Here  $n_{ij}$  represents the molecular field coefficients,  $C_{\rm R} = N_{\rm R} g^2 J (J+1) \mu_{\rm B}^2 / 3k_{\rm B}$ ,  $N_{\rm R}$  is the number of rare-earth atoms per unit volume,  $C_{\rm Co} = N_{\rm Co} 4S(S+1) \mu_{\rm B}^2 / 3k_{\rm B}$ ,  $N_{\rm Co}$  is the number of Co atoms per unit volume and  $\alpha = 2(g-1)/g$ . Neglecting  $T_{\rm R}$ ,  $T_{\rm C}$  is given by

$$T_{\rm C} = \{T_{\rm Co} + (T_{\rm Co}^2 + 4T_{\rm RCo}^2)^{1/2}\}/2$$
(5)

and,  $n_{CoCo}$  and  $n_{RCo}$ , can be calculated using

$$n_{\rm CoCo} = T_{\rm Co} / C_{\rm Co} \tag{6}$$

and

$$n_{\rm RCo} = \{T_{\rm C}(T_{\rm C} - T_{\rm Co}) / C_{\rm R} C_{\rm Co}\}^{1/2} / |\alpha|, \tag{7}$$

respectively.

Here, we calculated the molecular field coefficients,  $n_{\rm RCo}$ , and  $n_{\rm CoCo}$ , for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$  using the experimental values of  $T_{\rm C}$ . The dependence of the Curie temperature,  $T_{\rm C}$ , on the Co concentration for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$ and  $R_2Co_{14}B$  (R=Y, Sm and Gd) is shown in Fig. 1. The values of  $T_{\rm C}$  for RCo<sub>5</sub>, RCo<sub>4</sub>B,  $R_3Co_{11}B_4$ ,  $R_2Co_7B_3$ ,  $R_2Co_{17}$  and  $R_2Co_{14}B$  are from Refs. [9], [7,10], [7,11], [7,12], [9] and [13], respectively. The values of  $T_{\rm C}$  for R=Y are the smallest. The differences of the values of  $T_{\rm C}$ between those of R=Y and those of R=Sm and Gd for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3) are larger than those for  $RCo_5$ ,  $R_2Co_{17}$  and  $R_2Co_{14}B$ . Taking the value of  $T_{\rm C}$  for the Y compounds as  $T_{\rm Co}$ ,  $n_{\rm CoCo}$  can be deduced using Eq. (6). Then  $n_{\rm RCo}$  can be obtained by substituting the



Fig. 1. The dependence of the Curie temperature  $(T_{\rm C})$  on the Co concentration for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$  (R=Y, Sm and Gd).

appropriate  $T_{\rm C}$  data of each rare-earth compound into Eq. (7).

The value of  $n_{\rm RR}$  deduced from the ordering temperature for R–Ni compounds is 226 (Oe cm<sup>3</sup>/emu) [1]. That is much smaller than the calculated  $n_{\rm CoCo}$  and  $n_{\rm RCo}$  values for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$ .

The dependence of  $n_{\rm SmCo}$ ,  $n_{\rm GdCo}$ ,  $n_{\rm CoCo}$  and Co moment,  $\mu_{Co}$ , on the B concentration for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$  is shown in Fig. 2. The values of  $n_{\rm SmCo}$  and  $n_{\rm GdCo}$ , are those of  $n_{\rm RCo}$  for R=Sm and Gd, respectively and the values of  $n_{
m CoCo}$  and  $\mu_{
m Co}$  are those for R=Y. The values of  $\mu_{Co}$  for YCo<sub>5</sub>, YCo<sub>4</sub>B, Y<sub>3</sub>Co<sub>11</sub>B<sub>4</sub>,  $Y_2Co_7B_3$ ,  $Y_2Co_{17}$  and  $Y_2Co_{14}B$  are from Refs. [9], [7,10], [7,11], [7,12], [9] and [13], respectively. The value of  $n_{CoCo}$  decreases with increasing B content. The values of  $n_{\text{SmCo}}$  and  $n_{\text{GdCo}}$  decrease for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3) with increasing B content. In rare-earth transition-metal compounds, the exchange coupling of localized 4f and itinerant 3d moments is indirectly promoted via a local 4f-5d interaction combined with an interatomic 5d-3d interaction [14]. The 2p electrons of B lower the density of 3d states at the Fermi level by the 3d-2p hybridization [15] and the values of Co 3d moment decrease, which reduces the effect of 5d-3d hybridization and weakens the 4f–3d exchange interaction, therefore  $n_{GdCo}$  decreases. The values of  $n_{\rm RCo}$  (R=Sm and Gd) for RCo<sub>5</sub>, R<sub>2</sub>Co<sub>17</sub> and  $R_2Co_{14}B$  are small in spite of the small B concentration or



Fig. 2. The dependence of  $n_{\text{SmCo}}$ ,  $n_{\text{GoCo}}$ ,  $n_{\text{CoCo}}$  and Co moment,  $\mu_{\text{Co}}$ , on the B concentration for  $R_{n+1}\text{Co}_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2\text{Co}_{17}$  and  $R_2\text{Co}_{14}\text{B}$ .

the absence of B atoms. For those compounds, the Co–Co interaction is strong. The dependence of  $n_{\rm CoCo}$  on the B concentration is similar to that of  $\mu_{\rm Co}$ . The values of  $n_{\rm CoCo}$  and  $\mu_{\rm Co}$  for YCo<sub>5</sub>, Y<sub>2</sub>Co<sub>17</sub> and Y<sub>2</sub>Co<sub>14</sub>B are large. The values of  $n_{\rm CoCo}$  are approximately proportional to those of  $T_{\rm C}$ .

The dependence of  $n_{\text{SmCo}}$ ,  $n_{\text{GdCo}}$ ,  $n_{\text{CoCo}}$  and  $\mu_{\text{Co}}$  on the Co concentration for  $R_{n+1}\text{Co}_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2\text{Co}_{17}$  and  $R_2\text{Co}_{14}B$  is shown in Fig. 3. The values of



The dependence of  $n_{\rm SmCo}$ ,  $n_{\rm GdCo}$  and  $n_{\rm CoCo}$  on the R concentration for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$  is shown in Fig. 4. The values of  $n_{\rm GdCo}$  and  $n_{\rm CoCo}$  approximately decrease with increasing R content. On the contrary, the value of  $n_{\rm SmCo}$  increases with increasing Sm content. In  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3), for the same R concentration, the values of  $n_{\rm SmCo}$  and  $n_{\rm GdCo}$  and  $n_{\rm CoCo}$  are distributed over a wide range. The value of  $n_{\rm CoCo}$  for YCo<sub>5</sub> is much larger considering the Y content. The decrease in the values of  $n_{\rm CoCo}$  is larger than that of  $n_{\rm GdCo}$ .

A plot of  $n_{GdCo}$  versus  $\mu_{Co}$  for  $Gd_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $Gd_2Co_{17}$  and  $Gd_2Co_{14}B$  is shown in Fig. 5. The values of  $\mu_{Co}$  are obtained by assuming that the Gd moment is 7  $\mu_B$  and couples with the Co moment ferrimagnetically. The values of  $n_{GdCo}$  are approximately proportional to those of  $\mu_{Co}$  for  $Gd_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3) and for  $GdCo_5$ ,  $Gd_2Co_{17}$  and  $Gd_2Co_{14}B$ .

A plot of  $n_{\text{CoCo}}$  versus  $\mu_{\text{Co}}$  for  $Y_{n+1}\text{Co}_{3n+5}B_{2n}$  (n=0, 1, 1)



Fig. 3. The dependence of  $n_{\rm SmCo}$ ,  $n_{\rm GdCo}$ ,  $n_{\rm CoCo}$  and  $\mu_{\rm Co}$  on the Co concentration for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2Co_{17}$  and  $R_2Co_{14}B$ .



Fig. 4. The dependence of  $n_{\text{SmCo}}$ ,  $n_{\text{GdCo}}$  and  $n_{\text{CoCo}}$  on the R concentration for  $R_{n+1}\text{Co}_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $R_2\text{Co}_{17}$  and  $R_2\text{Co}_{14}B$ .



Fig. 5. A plot of  $n_{GdCo}$  versus  $\mu_{Co}$  for  $Gd_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $Gd_2Co_{17}$  and  $Gd_2Co_{14}B$ .

2, 3),  $Y_2Co_{17}$  and  $Y_2Co_{14}B$  is shown in Fig. 6. The values of  $n_{CoCo}$  increase with increasing  $\mu_{Co}$ . The values of  $n_{CoCo}$ for YCo<sub>5</sub>,  $Y_2Co_{17}$  and  $Y_2Co_{14}B$  are much too large considering the values of  $\mu_{Co}$ . The value of  $n_{CoCo}$  for



Fig. 6. A plot of  $n_{CoCo}$  versus  $\mu_{Co}$  for  $Y_{n+1}Co_{3n+5}B_{2n}$  (n=0, 1, 2, 3),  $Y_2Co_{17}$  and  $Y_2Co_{14}B$ .

 $Y_2Co_{14}B$  is large in spite of the presence of B atom, because the distance between B and Co is long and therefore the value of  $\mu_{Co}$  is large (see also Fig. 8).

In view of the different types of unit cells associated with the corresponding crystal structures, we have rewritten the formula composition as  $\text{RCo}_m\text{B}_n$  and used the lattice constants to calculate the volume, *V*, occupied by one formula unit  $\text{RCo}_m\text{B}_n$ . The values of lattice constants *a* and *c* for  $\text{RCo}_5$ ,  $\text{RCo}_4\text{B}$ ,  $\text{R}_3\text{Co}_{11}\text{B}_4$ ,  $\text{R}_2\text{Co}_7\text{B}_3$ ,  $\text{R}_2\text{Co}_{17}$  and  $\text{R}_2\text{Co}_{14}\text{B}$  are from Refs. [9], [7,10], [7,11], [7,12], [9] and [13], respectively. This *V* depends on the distance between R and Co. Next, we have rewritten the formula composition as  $\text{R}_m\text{Co}_n\text{B}$  and used the lattice constants to calculate the volume, *V*, occupied by one formula unit  $\text{R}_m\text{Co}_n\text{B}$ . This *V* depends on the distance between Co and B.

The values of  $n_{\rm SmCo}$  and  $n_{\rm GdCo}$  plotted versus the corresponding reciprocal values of the normalized two types of volume per formula unit RCo<sub>m</sub>B<sub>n</sub> and R<sub>m</sub>Co<sub>n</sub>B for R<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub> (n=0, 1, 2, 3), R<sub>2</sub>Co<sub>17</sub> and R<sub>2</sub>Co<sub>14</sub>B are shown in Fig. 7.

When V is the volume per formula unit  $\text{RCo}_m B_n$ , the values of  $n_{\text{GdCo}}$  almost decrease with increasing  $V^{-1}$ , but those of  $n_{\text{SmCo}}$  increase. The change in the values of  $n_{\text{SmCo}}$  is larger than that of  $n_{\text{GdCo}}$ . Consequently, with decreasing distances between R and Co, the value of  $n_{\text{SmCo}}$  increases, which is consistent with the result that the value of  $n_{\text{SmCo}}$  increases with increasing Sm content as shown in Fig. 4.



Fig. 7. The values of  $n_{\rm SmCo}$  and  $n_{\rm GdCo}$  plotted versus the corresponding reciprocal values of the normalized two types of volume per formula unit RCo<sub>m</sub>B<sub>n</sub> and R<sub>m</sub>Co<sub>n</sub>B for R<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub> (n=0, 1, 2, 3), R<sub>2</sub>Co<sub>17</sub> and R<sub>2</sub>Co<sub>14</sub>B.

On the contrary, the value of  $n_{GdCo}$  decreases. In Ref. [16], the values of  $n_{ErCo}$  for  $ErCo_3$ ,  $Er_2Co_7$ ,  $ErCo_4B$ ,  $ErCo_{5.8}$ ,  $Er_2Co_{14}B$ ,  $Er_2Co_{17}$  and  $ErCo_{12}B_6$  are roughly proportional to those of  $V^{-1}$ . This has been explained in Ref. [16] by assuming that with decreasing V, the 5d–3d hybridization increases and the 4f–3d exchange interaction increases.

When V is the volume per formula unit  $R_m Co_n B$ , the values of  $n_{SmCo}$  and  $n_{GdCo}$  decrease with increasing  $V^{-1}$  except for those of  $R_2Co_{14}B$ . Therefore, with decreasing distances between B and Co, the values of  $n_{SmCo}$  and  $n_{GdCo}$  decrease for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3). When the distance between B and Co becomes small, the 3d–2p hybridization increases and the 3d moment decreases, consequently the 5d–3d hybridization decrease of the 5d–3d hybridization due to the decreasing 3d moment is larger than the increase of the 5d–3d hybridization due to the decrease of V for R=Gd.

The values of  $\mu_{Co}$  plotted versus the corresponding normalized cube root of the volume per formula unit YCo<sub>m</sub>B<sub>n</sub> and per formula unit Y<sub>m</sub>Co<sub>n</sub>B for Y<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub> (n=0, 1, 2, 3), Y<sub>2</sub>Co<sub>17</sub> and Y<sub>2</sub>Co<sub>14</sub>B are shown in Fig. 8. In both cases, the values of  $\mu_{Co}$  are apparently proportional to those of the cube root of V. The decrease of  $\mu_{Co}$  is particularly large for decreasing values of V<sup>1/3</sup> in the YCo<sub>m</sub>B<sub>n</sub> compounds. These results suggest that the values of  $\mu_{Co}$  are proportional to the distances between Y and Co, and Co and B. The values of  $n_{CoCo}$  plotted versus the corresponding reciprocal values of the normalized two types of volume per formula unit YCo<sub>m</sub>B<sub>n</sub> and per formula unit Y<sub>m</sub>Co<sub>n</sub>B for Y<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub> (n=0, 1, 2, 3), Y<sub>2</sub>Co<sub>17</sub> and Y<sub>2</sub>Co<sub>14</sub>B are shown in Fig. 9. In both cases, the values of  $n_{CoCo}$ decrease with increasing values of  $V^{-1}$ . With increasing distances between Y and Co, and Co and B, the values of  $\mu_{Co}$  increase (Fig. 8) and also the values of  $n_{CoCo}$  increase (Fig. 9). For Y<sub>2</sub>Co<sub>14</sub>B [17], the distances between Co at four sites and B are large, so there are relatively more Co atoms with large moments.

The discussion of the 3d magnetization in rare-earth intermetallics can be performed within the simple concept of magnetic valence  $Z_m$  [18]. Within the magnetic valence model, the magnetic moment of an alloy is considered in terms of magnetic moment, M, averaged over all atoms in the alloy. The mean magnetic moment per atom M is expressed as

$$M = Z_{\rm m} + 2N_{\rm sp}^{\uparrow}.\tag{8}$$

Here  $Z_{\rm m}$  is the magnetic valence;  $2N_{\rm sp}^{\uparrow}$  is the number of s and p electrons in the spin-up-state band. The values of  $N_{\rm sp}^{\uparrow}$  usually range from 0.3 to 0.45 [18].  $Z_{\rm m}$  is expressed as

$$Z_{\rm m} = 2N_{\rm d}^{\dagger} - Z. \tag{9}$$

Here  $N_d^{\mathsf{T}}$  is the number of electrons in the spin-up band and *Z* is the chemical valence. To apply the magnetic valence

Fig. 8. The values of  $\mu_{Co}$  plotted versus the corresponding normalized cube root of the volume per formula unit YCo<sub>m</sub>B<sub>n</sub> and per formula unit Y<sub>m</sub>Co<sub>n</sub>B for Y<sub>n+1</sub>Co<sub>3n+5</sub>B<sub>2n</sub> (n=0, 1, 2, 3), Y<sub>2</sub>Co<sub>17</sub> and Y<sub>2</sub>Co<sub>14</sub>B.

Fig. 9. The values of  $n_{\text{CoCo}}$  plotted versus the corresponding reciprocal values of the normalized two types of volume per formula unit  $\text{YCo}_m\text{B}_n$  and per formula unit  $\text{Y}_m\text{Co}_n\text{B}$  for  $\text{Y}_{n+1}\text{Co}_{3n+5}\text{B}_{2n}$  (n=0, 1, 2, 3),  $\text{Y}_2\text{Co}_{17}$  and  $\text{Y}_2\text{Co}_{14}\text{B}$ .







Fig. 10. The experimental magnetic moment as a function of magnetic valence for Y–Co–B, Y–Co, Y–Co–Fe–B, Fe, Co and Ni and the calculated moments with  $N_{\rm sp}^{\uparrow} = 0.45$ , with strong ferromagnetism, in Eq. (8).

model, the Y–Co–B series can be rewritten as  $Y_{v1}Co_{1-v}B_{v2}$  (y = y1 + y2). Then  $Z_m$  is expressed as

$$Z_{\rm m} = 2N_{\rm d}^{\uparrow} (1-y) - Z_{\rm Co}(1-y) - (Z_{\rm Y}y1 + Z_{\rm B}y2).$$
(10)

Here  $N_d^{\text{T}}$  is taken to be the value for a strong ferromagnet (=5). The values of chemical valence are  $Z_{\text{Co}} = 9$ ,  $Z_{\text{Y}} = 3$ ,  $Z_{\text{B}} = 2$  [18].

The experimental magnetic moment as a function of magnetic valence for Y-Co-B, Y-Co, Y-Co-Fe-B, Fe, Co and Ni and the calculated moments with  $N_{sp}^{\uparrow} = 0.45$ , with strong ferromagnetism, in Eq. (8) are presented in Fig. 10. The values of the experimental magnetic moment for  $Y_2(Co_{1-x}Fe_x)_{14}B$ ,  $Y_2Co_{14}B_{0.75}$  and  $Y_2Co_{16}B$  are from Refs. [19,20] and [17], respectively. For  $Y_{n+1}Co_{3n+5}B_{2n}$ (n=1, 2, 3), the experimental magnetic moment is below the calculated one, which shows that weak ferromagnetism is present. For YCo<sub>5</sub> and Y<sub>2</sub>Co<sub>17</sub>, the experimental magnetic moment is near the calculated one, hence whose compounds show strong ferromagnetism. For  $Y_2(Co_{1-x}Fe_x)_{14}B$ , a transition from weak to strong ferromagnetism occurs as x increases from 1 to 0.9.

### 3. Conclusions

We calculated the molecular field coefficients,  $n_{\rm RCo}$ , (R=Sm and Gd) and  $n_{\rm CoCo}$  (R=Y) for  $R_{n+1}Co_{3n+5}B_{2n}$  (*n*=0, 1, 2, 3), R<sub>2</sub>Co<sub>17</sub> and R<sub>2</sub>Co<sub>14</sub>B using the experimental values of the Curie temperature.

With increasing B content, the value of  $n_{CoCo}$  decreases. The values of  $n_{SmCo}$  and  $n_{GdCo}$  decrease for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3). With increasing Co content, the values of  $n_{SmCo}$  and  $n_{GdCo}$  increase for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3) and decrease for  $RCo_5$ ,  $R_2Co_{17}$  and  $R_2Co_{14}B$  and those of  $n_{CoCo}$  increase. With increasing R content, the values of  $n_{GdCo}$  and  $n_{CoCo}$  approximately decrease, but the value of  $n_{SmCo}$  increases.

With decreasing distances between R and Co, the value of  $n_{\rm SmCo}$  increases and that of  $n_{\rm GdCo}$  decreases. With decreasing distances between B and Co, the values of  $n_{\rm SmCo}$  and  $n_{\rm GdCo}$  decrease for  $R_{n+1}Co_{3n+5}B_{2n}$  (n=1, 2, 3).

The values of  $\mu_{Co}$  are proportional to the distances between Y and Co, and Co and B. With increasing distances, the values of  $\mu_{Co}$  increase and those of  $n_{CoCo}$ increase.

The tendency of the values of  $n_{\text{RCo}}$  and  $n_{\text{CoCo}}$  for  $R_{n+1}\text{Co}_{3n+5}B_{2n}$  (n=1, 2, 3) is different from that for RCo<sub>5</sub>, R<sub>2</sub>Co<sub>17</sub> and R<sub>2</sub>Co<sub>14</sub>B.

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